

# 2.2 Circles

## Question Paper

Course	CIEAS Maths
Section	2. Coordinate Geometry
Topic	2.2 Circles
Difficulty	Very Hard

**Time allowed:** 70  
**Score:** /54  
**Percentage:** /100

**Question 1**

The points  $A(2, -21)$  and  $B(-5, 3)$  are the two endpoints of the diameter  $AB$  of a circle. Find the equation of the circle in the form  $ax^2 + ay^2 + bx + cy + d = 0$ , where  $a, b, c$  and  $d$  are integers to be found.

[6 marks]

**Question 2**

Find the centre and radius of the circle with equation  $x^2 + y^2 + x - 3y + 2 = 0$

[4 marks]

**Question 3**

The line  $x + y = c$  intersects the circle  $x^2 + y^2 - 6x + 10y - 16 = 0$  at exactly two points. Find the range of possible values of  $c$ .

[7 marks]

**Question 4**

The points  $A(-2, 3)$ ,  $B(0, 6)$  and  $C(k, -1)$  lie on a circle, where  $BC$  is the diameter of the circle.

Find the value of  $k$ .

[4 marks]

**Question 5**

A circle  $C$  has equation  $x^2 + y^2 - 10x - 4y + 19 = 0$ . Point  $P$  lies on the circle, and the tangent to the circle at point  $P$  has a gradient of  $-3$ . Find the two possible sets of coordinates for point  $P$ .

[7 marks]

**Question 6**

The points  $A(4, 6)$ ,  $B(7, 2)$  and  $C(12, 12)$  lie on a circle.

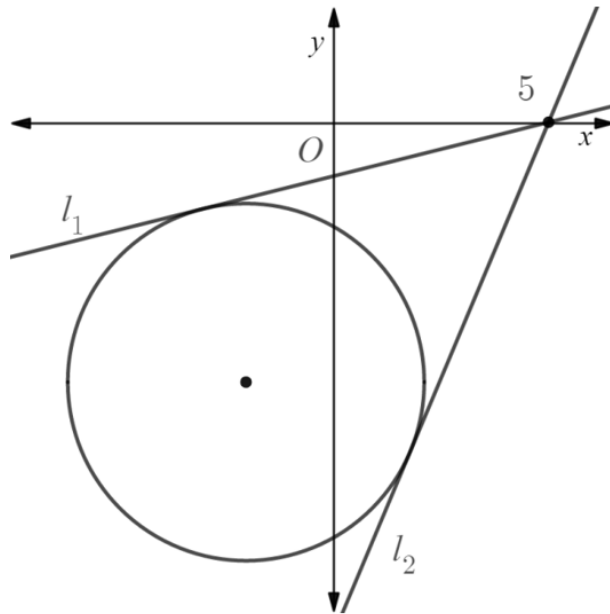
Find the equation of the circle

**[7 marks]**

**Question 7**

A circle has equation  $x^2 + y^2 + 4x + 12y = -23$ .

The lines  $l_1$  and  $l_2$  are both tangents to the circle, and they intersect at the point  $(5, 0)$ .

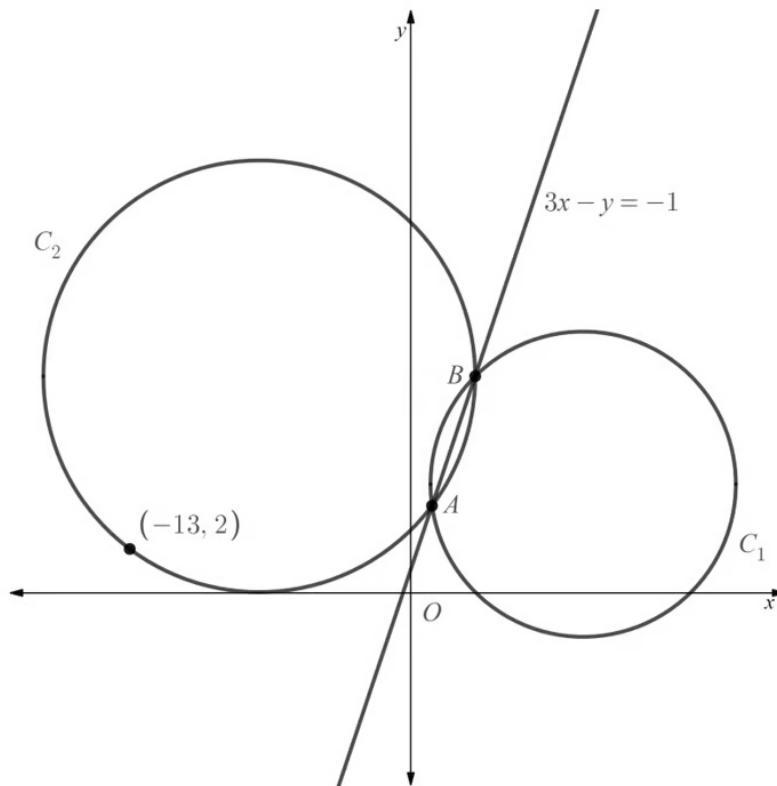


Find the equations of  $l_1$  and  $l_2$ , giving your answers in the form  $y = mx + c$ .

[8 marks]

**Question 8**

The diagram below shows circles  $C_1$  and  $C_2$  which intersect at the two points  $A$  and  $B$ . Circle  $C_1$  has equation  $x^2 + y^2 - 16x - 10y + 39 = 0$ , and points  $A$  and  $B$  lie along the line with equation  $3x - y = -1$ . Circle  $C_2$  also passes through the point  $(-13, 2)$ .



Find an equation of circle  $C_2$ .

[11 marks]

